

Review of Week 1-7

- Week 1
 - Vector Manipulation, Addition, Subtraction, Unit Vector, Dot Product, Cross Product, Mixed Triple Product
- Week 2
 - Torque and moment, moment about a line, simplification (Wrench)
- Week 3: *Free Body diagrams*
- Week 4: *Objects & Systems in Equilibrium*
- Week 5: *Centroids and Center of Mass*
- Week 6: *Friction*
- Week 7: *Biomedical Applications*

1

Explicit Topics on Exam

- Week 1
 - Vector Manipulation, Addition, Subtraction, Unit Vector, Dot Product, Cross Product, Mixed Triple Product
- Week 2
 - Torque and moment, moment about a line, simplification (Wrench)
- Week 3: *Free Body diagrams*
- Week 4: *Objects & Systems in Equilibrium (2)*
- Week 5: *Centroids and Center of Mass*
- Week 6: *Friction (2)*
- Week 7: *Biomedical Applications (2)*

2

Exam

Next week (31 July):
3-hour Midterm on weeks 1-7
Assigned seats, *different* exams (so don't copy ☺)
Turn off phones, No bathroom breaks during exam
6 problems:
Three 2D problems
Three 3D problems

3

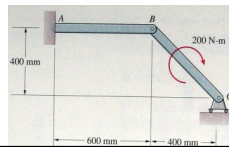
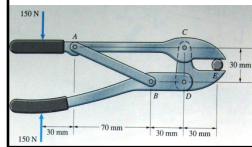
Formula Sheet

- Not required
- Must be original (Copying is not allowed)
- Must be typed, and include your name
- Must submit to Dr. Jon along with your exam
- 1 page, front and back
- See Syllabus for details

4

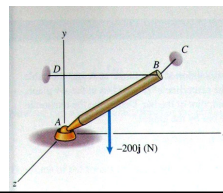
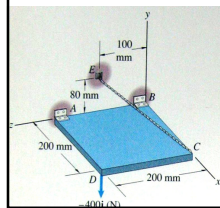
2D System Equilibrium

- 15 points
 - 13 points for math
 - 5 points for equal/opposite forces
 - 1 point for dimensions
 - 1 point for answer



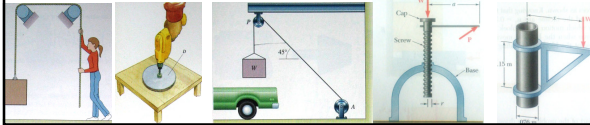
3D Equilibrium

- 20 points
 - 10 points for concepts
 - 6 points for math
 - 2 points for answers
 - 2 points for dimensions



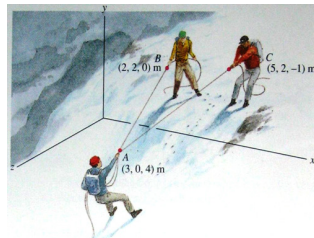
2D Friction

- 10 points



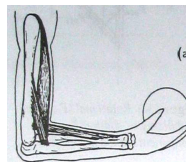
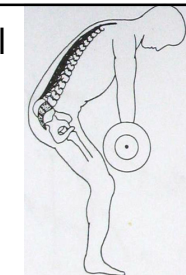
3D Friction

- 20 points
 - 13 for description
 - 7 for math



2D Biomedical

- 20 points
- Part A (5 points)
 - 3 points for math
 - 1 point for answer
 - 1 point for dimensions
- Part B (15 points)
 - 4 points for correct concept
 - 9 points for math
 - 1 point for answer
 - 1 point for dimensions



Remember

- Do not write in red ink
- Turn off all cell phones
- Do not use any device which can communicate with the internet (PDA, Palm Pilot, etc...)
- I highly recommend a calculator for this exam (borrow one if necessary)

13

Review

- 3D Biomechanics problem, again, using different methods

14

3D Example

The baseball player weighs 80 kg, (*no height given*).

The acceleration of the forearm and ball exert the following couple on the humerus bone:

$$M = -8\hat{i} + 5\hat{j} - 8\hat{k}$$

The rotator cuff muscles exert a -10 N-m couple parallel to the humerus going from the shoulder to the elbow.

Assume only 1 muscle acts at a proximal point 10% of the length of the humerus and 0.5 cm superior to center of the bone

Assume the muscle acts perpendicular to humerus

What force must that muscle generate?

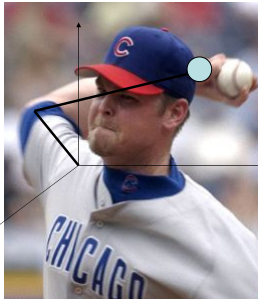


Anthropometry

- Weight of arm: $(.028)(80 \text{ kg})(9.81 \text{ m/s}^2) = 22\text{N}$
- COM: = $(0.436) * \text{Arm vector} + \text{shoulder}$

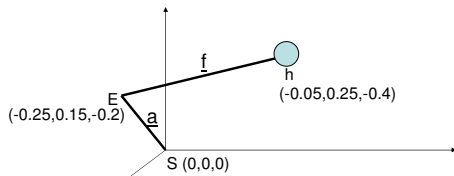
| Segment | Segment Weight / Total Body Weight | Segment Length / Height | Proximal COM / Segment Length |
|-------------|------------------------------------|-------------------------|-------------------------------|
| Upper Arm | 2.8% | A 18.6% | A1 43.6% |
| Forearm | 1.6% | B 14.6% | B1 43.0% |
| Hand | 0.6% | C 10.8% | C1 50.6% |
| Thigh | 10.0% | D 24.5% | D1 43.3% |
| Shank | 4.7% | E 24.6% | E1 43.3% |
| Foot | 1.5% | F 3.9% | F1 50.0% |
| Trunk | 49.7% | G 34.0% | G1 50.0% |
| Head & Neck | 8.1% | H 18.2% | |

Coordinates



17

Coordinates



18

Solution: What is the force?

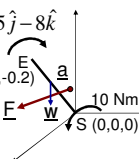
1) $M_E = -8\hat{i} + 5\hat{j} - 8\hat{k}$ $M_E = -8\hat{i} + 5\hat{j} - 8\hat{k}$

2) $M_S = -10\hat{i} + 7.07\hat{j} + 5.66\hat{k}$

$\underline{SE} = -0.25\hat{i} + 0.15\hat{j} - 0.2\hat{k}$ $(-0.25, 0.15, -0.2)$

$\hat{e}_{SE} = -0.707\hat{i} + 0.424\hat{j} - 0.566\hat{k}$

$\underline{M}_S = -10\hat{e}_{SE} = 7.07\hat{i} - 4.24\hat{j} + 5.66\hat{k}$



3) $M_W = r \times W = 0.436 \underline{SE} \times (-22\hat{j})$ } Different strategy

$$\underline{M}_W = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -0.106 & 0.06 & -0.085 \\ 0 & -20 & 0 \end{vmatrix}$$

$$\underline{M}_W = -1.7\hat{i} + 2.12\hat{k}$$

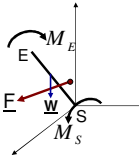
19

Solution: What is the force?

$M_E = -8\hat{i} + 5\hat{j} - 8\hat{k}$

$M_S = 7.07\hat{i} - 4.24\hat{j} + 5.66\hat{k}$

$\underline{M}_W = -1.7\hat{i} + 2.12\hat{k}$



$$\sum M_{pointS} = M_S + M_E + M_F + M_W = 0$$

$$M_F = 2.63\hat{i} - 0.76\hat{j} + 0.22\hat{k}$$

20

Solution: What is the force?

$M_F = 2.63\hat{i} - 0.76\hat{j} + 0.22\hat{k}$

$M_F = r \times F$

$r = 0.15\underline{SE} + 0.005\hat{j} = -0.25\hat{i} + 0.019\hat{j} - 0.2\hat{k}$

$$M_F = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -0.25 & 0.019 & -0.2 \\ F_x & F_y & F_z \end{vmatrix}$$

$$M_F = (0.019F_z + 0.02F_y)\hat{i} - (-0.25F_z + 0.02F_x)\hat{j} + (-0.25F_y - 0.019F_x)\hat{k}$$

$\hat{i}: 0.019F_z + 0.02F_y = 2.63$

$\hat{j}: 0.025F_z - 0.02F_x = -0.76$

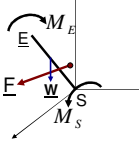
$\hat{k}: -0.025F_y - 0.019F_x = 0.22$

This solution is never solvable

Equations are not independent

Infinite Number of Answers

21



Infinite Answers

- Last class: I added constraint: $F_z=0$ (easier to understand).
- This class: I added constraint: "Force acts perpendicular to humerus" (Less ambiguous)
- Understand that your 3 equations will never be solvable. Use whatever solution I give you. (I will either say set F_z equal to 0, or Force acts perpendicular or parallel to some axis or plane)

22

Force Acts Perpendicular

- If force acts perpendicular to humerus, use dot product:

$$\cos \theta = \frac{\underline{A} \cdot \underline{B}}{|\underline{A}| |\underline{B}|}$$

$$0 = \frac{\underline{A} \cdot \underline{B}}{|\underline{A}| |\underline{B}|}$$

$$\underline{A} \cdot \underline{B} = 0$$

$$\underline{E}_M \cdot \underline{SE} = 0 \quad \underline{SE} = -0.25\hat{i} + 0.15\hat{j} - 0.2\hat{k}$$

$$-0.25F_{Mx} + 0.15F_{My} - 0.2F_{Mz} = 0$$

- This provides extra Equation. Now we can solve.
- Note: This is not the answer; it is 1 of the 3 necessary equations

23

Solving Equations

$$\hat{i}: 0.019F_z + 0.02F_y = 2.63$$

$$\hat{j}: 0.025F_z - 0.02F_x = -0.76$$

$$\hat{k}: -0.025F_y - 0.019F_x = 0.22$$

$$\text{Perpendicular: } -0.25F_x + 0.15F_y - 0.2F_z = 0$$
